

Garfield School Calculation Policy

- Garfield School follows the White Rose Maths scheme.
- This policy mostly uses strategies taken from the White Rose Maths Scheme although a few areas have been altered in line with previous good practice taught at Garfield.
- This calculation policy follows the CPA learning approach (Concrete, Pictorial and Abstract).
- Concrete means to use physical objects to solve maths problems.
- Pictorial is to use drawings or picture representations.
- Abstract is to solve maths problems using only numbers.
- In EYFS, concrete and pictorial methods are mainly used. There is no expectation for children to be able to record a number sentence.
- In KS1 the majority of calculations taught involve concrete methods and children gradually become more familiar with pictorial and some simple abstract representations.
- The methods outlined for the earlier years in KS2 (Years 3 and 4) are more pictorial, i.e., they break down the calculations so that the children understand how they are manipulating the numbers to calculate the answer. Children gradually learn how to relate these pictorial representations to more abstract calculations.
- The children move on to more formal abstract calculations in Years 5 and 6.
- In Year 2, pupils are taught the 2, 5 and 10 times tables. In Year 3, the 3, 4 and 8 times tables are introduced and by the end of Year 4, pupils are expected to know all of the times tables up to 12 by 12. At the end of Year 4, pupils have to take part in a National Multiplication Check.

be manipulated.



Pictorial Objective Concrete Abstract Knows that a group of 5+2=7things change in quantity when something is added. Find the total number part Use toys and general classroom resources of items in two groups for children to physically manipulate, group by counting all of them. whole and regroup quantities. Says the number that is part one more than a given number. Finds one more from a group of up to five objects, then ten objects. In practical activities Two groups of pictures so children are able to and discussion, count the total visually. beginning to use the A focus on symbols and numbers to form a vocabulary involved in calculation. adding. Use specific maths resources such a snap *No expectation for children to be able to Using quantities and cubes, Numicon, bead strings to support record a number sentence or objects, they add two with adding. addition/subtraction calculation. single digit numbers 5 and count on to find the 3 Marbles answer. 1 Marble Solve problems including doubling. Bar model using visuals, pictures and icons or colours. Use visual supports such as ten frames, part-part-whole and addition mats, with the physical objects and resources that can

Objective	Concrete	Pictorial	Abstract
Objective	Concrete	Use visual supports such as ten frames, part-part-whole and addition mats with pictures and icons.	ADSTRACT



Pictorial Objective Concrete Abstract Knows that a group of 10-1-? things change in quantity when something is taken away 10 - 6 = 4Use toys and general classroom resources Find one less from a for children to physically manipulate, group group of five objects, and regroup quantities. 3 then ten objects. 7 In practical activities 7 - 3 = ?and discussion, A group of pictures for children to cross out or beginning to use the cover quantities to support subtraction. vocabulary involved in subtracting. Use specific maths resources such a snap Using quantities and A focus on symbols and numbers to form a cubes, Numicon, bead strings to support objects, they subtract calculation. with subtracting. two single digit numbers and count *No expectation for children to be able to back to find the record a number sentence or answer. addition/subtraction calculation. Use visual supports such as ten frames, part-partwhole and bar models with pictures and icons. Use visual supports such as ten frames, part-part-whole and subtraction mats, with the physical objects and resources that can be manipulated.

EYFS Calculation Guidance: Multiplication

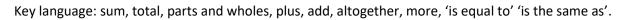


Objective	Concrete	Pictorial	Abstract
Solve problems including doubling	Counting and other maths resources for children to make 2 equal groups. Physical and real life examples that encourage children to see concept of doubling as adding two equal groups.	Pictures and icons that encourage children to see concept of doubling as adding two equal groups.	1+1= 7+7= 2+2= 8+8= 3+3= 9+9= 4+4= 10+10= 5+5= 11+11= 6+6= 12+12= Addition calculations to model adding two equal groups.



Objective	Concrete	Pictorial	Abstract
Solve problems including halving and sharing. Halving a whole, halving a quantity of objects. Sharing a quantity of objects.	Children have the opportunity to physically cut objects, food or shapes in half. Counting and other maths resources for children who share into two equal groups.	Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. For example, knowing 4 is made up of 2 groups of 2 – so half of 4 is 2. Bar model with pictures or icons to support understanding of finding 2 equal parts of a number, to further understand how two halves make a whole. Pictures for children to create and visualise 3 or more equal groups.	

Objective	Concrete	Pictorial	Abstract
	Use visual supports such as halving mats and part-part-whole, with the physical objects and resources that can be manipulated. Counting and other maths resources for children to explore sharing between 3 or more.		





	Objective	Concrete	Pictorial	Abstract
	Number bonds of 5, 6, 7, 8, 9 and 10	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	2+3=5 3+2=5 5=3+2 5=2+3 Use the part-part-whole diagram as shown above to move into the abstract.
Year 1	Counting	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Use a number line to count on in ones. 5 6 7 8	whole 2 part 5 + 3 = 8
	8	5 6 7 8 4 5 6	A bar model which encourages the children to count on, rather than count all.	The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? 4+2

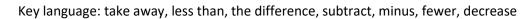
	Objective	Concrete	Pictorial	Abstract
Year 1	Regrouping to make 10	6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.	6+5=11 4 1 6+4=10	Children to develop an understanding of equality e.g. $6 + \Box = 11$ $6 + 5 = 5 + \Box$ $6 + 5 = \Box + 4$
Year 2	Adding 3 single digit numbers	4 + 7 + 6 = 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.



	Objective	Concrete	Pictorial	Abstract
	Column method without regrouping	Add together the ones first, then add the tens. Use the Base 10 blocks first before moving onto place value counters. 24 + 15 = 44 + 15 =	After physically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. 10s 1s	24 + 15 = 39 24 + 15 39
	Column met		• • • • •	
Year 2	Column method with regrouping	Add up the units and exchange 10 ones for 1 ten.	Using place value counters, children can draw the counters to help them to solve additions. 10s 1s 10s 1s 10s 1s	40 + 9 20 + 3 60 + 12 = 72



	Objective	Concrete	Pictorial	Abstract
		Make both numbers on a place value grid.	100s 10s 1s	100 + 40 + 6 500 + 20 + 7 600 + 70 + 3 = 673
Year 3/4	Column method with regrouping	Add up the units and exchange 10 ones for 1 ten. As children move on to decimals, money and decimal place value counters can be used to support learning. NB By Year 4 children will progress on to adding four digit numbers.	100s 10s 1s Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding. NB Addition of money needs to have £ and p added separately.	As the children progress, they will move from the expanded to the compacted method. 146 + 527 673 1 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.
Year 5/6	Column method with regrouping	Consolidate understanding using numbers	with more than 4 digits and extend by addir	ng numbers with up to 3 decimal places.





	Objective	Concrete	Pictorial	Abstract
	Taking away ones	Use physical objects, counters, cubes etc. to show how objects can be taken away. 4 - 2 = 2	Cross out drawn objects to show what has been taken away. 4 - 2 = 2	4 – 2 = 2
Year 1	Counting back	Counting back (using number lines or number tracks) children start with 6 and count back 2. 6 - 2 = 4 1 2 3 4 5 6 7 8 9 10	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number, showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Find the difference	Compare amounts and objects to find the difference. ? Use cubes to build towers or make bars to find the difference. Use basic bar models with items to find the difference.	Count on to find the difference. Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 ? Lisa Sister 22 Draw bars to find the difference between 2 numbers.	Hannah has 8 goldfish. Helen has 3 goldfish. Find the difference between the number of goldfish the girls have.



	Objective	Concrete	Pictorial	Abstract
Year 2	Column method without regrouping	Use Base 10 to make the bigger number then take the smaller number away.	Draw the Base 10 or place value counters alongside the written calculation to help to show working.	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ This will lead to a clear written column subtraction.
	Column met	Show how you partition numbers to subtract. Again make the larger number first.	Calculations 176 - 64 = 176 - 64 - 112	20



	Objective	Concrete	Pictorial	Abstract
Year 3 onwards	Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters	Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident, children can find their own way to record the exchange/regrouping. Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup. 42 - 18 = 24 3	Children can start their formal written method by partitioning the number into clear place value columns. This will lead to an understanding of subtracting any number including decimals. 5 12 1 2 6 3 0 0 - 2 6 5 2 3 6 5 5



	Objective	Concrete	Pictorial	Abstract
Year 3 up	Column method with regrouping	Now look at the tens, can I take away 8 tens easily? I need to exchange 1 hundred for 10 tens. Now I can take away 8 tens and complete my subtraction. Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.		Calculations 234 - 88 Calculations 234 - 88 146 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

Calculation Guidance: Multiplication

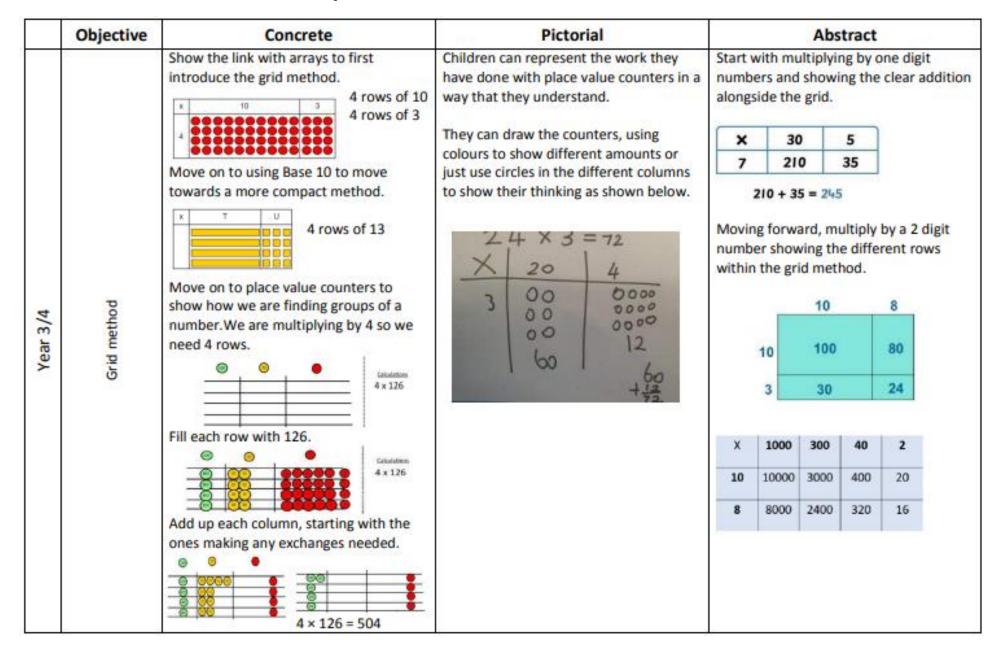


Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups, repeated addition.

	Objective	Concrete	Pictorial	Abstract		
Year 1/2	Repeated addition	Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2+2+2=6 5+5+5=15	Write addition sentences to describe objects and pictures. 2+2+2=6		
	Arrays- showing commutative multiplication	Create arrays using counters/cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences. 4 × 2 = 8 2 × 4 = 8 4 × 2 = 8 Link arrays to area of rectangles.	Use an array to write multiplication sentences and reinforce repeated addition. $ \begin{array}{cccccccccccccccccccccccccccccccccc$		



Calculation Guidance: Multiplication





Calculation Guidance: Multiplication

Objectiv	Concrete	Pictorial			Abstract			ct
Expanded method	Show the link with arrays to first introduce the expanded method. 10 8 10 80	× 10 3	000000 000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	the children	Start with long multiplication, reminding the children about lining up their numbers clearly in columns. 18 x 13 24 (3 x 8) 30 (3 x 10)) 80 (10 x 8) 100 (10 x 10)		
Year 5/6 Compact method	Children can continue to be supported by place value counters at the stage of multiplication. It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	learners who multiplication methods.	en solving probon alongside the	formal written	children abou clearly in colu If it helps, chil are solving ne	Start with long multiplication, reminding the children about lining up their numbers clearly in columns. If it helps, children can write out what they are solving next to their answer. 7 4 × 6 3 1 2 2 1 0 2 4 0 4 6 6 2 This moves to the more compact method. 13 4 2 x 18 13 4 2 0 10 7 3 6		



Key language: share, group, divide, divided by, half, repeated subtraction, equal groups, remainder.

	Objective	ective Concrete Pictorial		Abstract
	Sharing	I have 6 cubes, can you share them equally between two people?	Represent the sharing pictorially.	$6 \div 2 = 3$ 3 Children should also be encouraged to use their 2 times tables facts.
Year 1/2	Grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 10 1 2 3 4 5 6 7 8 9 10 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	10 ÷ 5 = 2 Divide 10 into 5 groups. How many are in each group?



	Objective	Concrete	Pictorial	Abstract
	Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 + 3 = 5 5 x 3 = 15 15 + 5 = 3 3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. 5 x 3 = 15 3 x 5 = 15 15 ÷ 5 = 3 15 ÷ 3 = 5
Year 3/4	Short division		Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently. Students can then progress onto dividing using numberlines (with no remainders) Eg 15 ÷ 3 = 5 0 5 10 15 (1x5) (1x5) (1x5) = 3 lots of 5 15 ÷ 3 = 5 (as 5 x 3 = 15)	Begin with divisions that divide equally with no remainder. 2 1 8 3 4 8 7 2



	Objective	Concrete	Pictorial	Abstract	
Year 3/4	14 ÷ 3 = Divide objects between groups and see how much is left over		Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. Draw dots and group them to divide an amount and clearly show a remainder.	Complete written divisions and show the remainder using r. 29 + 8 = 3 REMAINDER 5 ↑ ↑ ↑ ↑ ↑ dividend divisor quotient remainder	
Year 5/6	Short division with remainders	364 ÷ 3 = 121 rem 1 3 364		Move onto divisions with a remainder. Once children understand remainders, begin to express as a fraction or decimal according to the context. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	



	Objective	Concrete	Pictorial	Abstract
Year				$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
>		When the divisor is greater than 10, pupils will need to use short multiplication to calculate how many times the divisor fits into the dividend.	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	